

*Extreme  
value*

Determine the maximum and minimum velocity of the function given

$$2) v(t) = t^3 - 3t^2 + 4 \quad [0, 4]$$

$$v(0) = 4$$

$$v'(t) = a(t) = 3t^2 - 6t$$

$$v(2) = 8 - 12 + 4 = 0$$

$$0 = 3t^2 - 6t$$

$$v(4) = 64 - 48 + 4 = 20$$

$$0 = 3t(t - 2)$$

$$t=0 \quad t=2$$

(2, 0) Abs Min

(4, 20) Abs Max

Determine the maximum and minimum acceleration of the function given

$$5) v(t) = 4t^2 - 6t^3 \quad [0, 3]$$

$$a(t) = v'(t) = 8t - 18t^2$$

$$a(0) = 0$$

$$a\left(\frac{2}{9}\right) = 8\left(\frac{2}{9}\right) - 18\left(\frac{2}{9}\right)^2$$

$$= \frac{16}{9} - \frac{18\left(\frac{4}{81}\right)}{1\left(\frac{81}{81}\right)}$$

$$= \frac{16}{9} - \frac{2\left(\frac{4}{9}\right)}{\cancel{1\left(\frac{81}{81}\right)}}$$

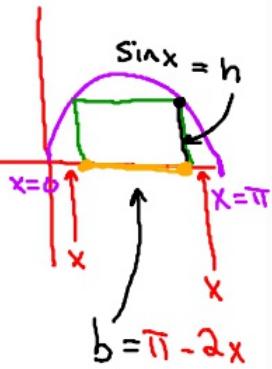
$$= \frac{16}{9} - \frac{8}{9} - \frac{8}{9}$$

$$a(3) = -138$$

Maximize  
minimize

$$y = \sin x \rightarrow \text{height}$$

What you'll Learn About:  
How to use derivatives to solve real world problems



- A) A rectangle is to be inscribed under one arch of the sine curve. What is the largest area the rectangle can have, and what dimensions give that area.

$$A'(0.5) = 0.920 > 0$$

$$A'(1) = -1.066 < 0$$

$$A'(2.5) = 0.290 > 0$$

Take derivative of

$$A = l w \quad A = b h$$

$$A = (\pi - 2x) \sin x$$

$$A'(x) = (\pi - 2x) \cos x + \sin x (-2)$$

*Loc Max*  
b/c  $A'$  changes from + to -

$$0 = (\pi - 2x) \cos x - 2 \sin x$$

$$x = 0.710, 2.431 \text{ and } \pi(0.710) > 0$$

$$A = (\pi - 2(0.710))(\sin(0.710))$$

- B) A rectangle is to be inscribed between the curve  $y = 25 - x^2$  and the x-axis. What is the largest area the rectangle can have, and what dimensions give that area.